

# RELIABILITY ENGINEERING PRINCIPLES

$$R_{1:n}(t) = \sum_{j=1}^n \frac{r_j^2}{r_j^2(n-j+1)} e^{-\lambda_j t} (1-p)^{n-j+1}$$

Exercising such machines from the failure rate increases, remains constant, gradually increases or considerably increases as a function of time.

Weibull Reliability Estimation

Effect of failure load on the probability of failure of a component under a constant load

$$R(t) = Ae^{-\lambda t}$$





# Reliability Indices

**Failure Rate ( $\lambda$ )**- A Reliability index that represents the **rate at which your product fails**.



**Mean Time To Failure (MTTF)** – The reliability index for **non-repairable units** represents the *mean time to failure*.

**Mean Time Between Failure (MTBF)** – The reliability index for **repairable units** represents the *mean time between failure*.

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$$\text{Failure Rate } (\lambda) = \frac{\text{Number of Failures}}{\text{Operating Time (Cycles)}} = \text{Failures Per Hour}$$

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# RELIABILITY INDICES

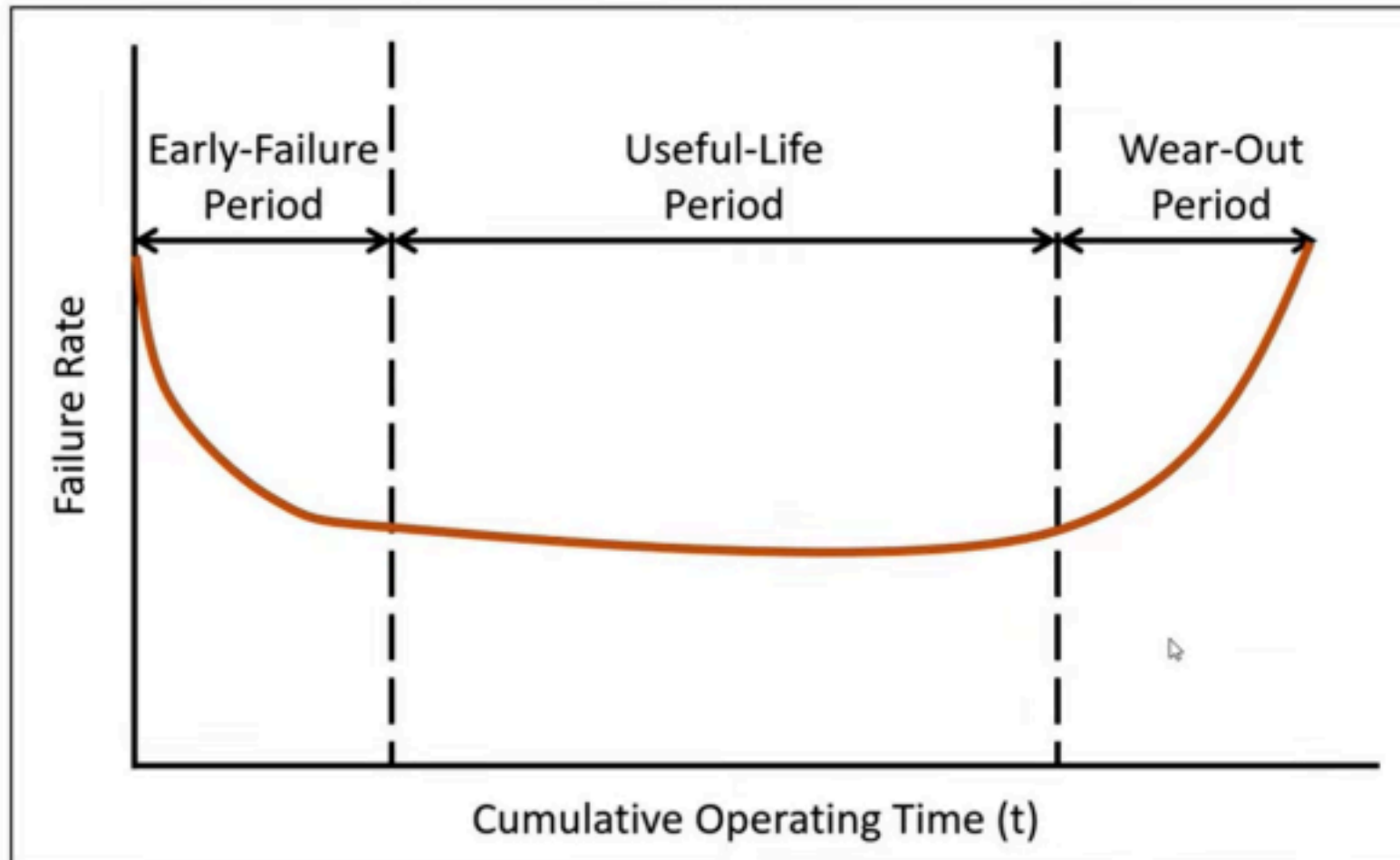
*Reliability:*  $R(t) = e^{-\lambda t}$

$$\lambda = \text{Failure Rate} = \frac{1}{\theta}$$

*Reliability:*  $R(t) = e^{-\left(\frac{t}{\theta}\right)}$

# The Bathtub Curve

The **bathtub curve** is a **reliability tool** that is used to **model the reliability of a unit** or system over the units **entire life**.



## Reliability @ Different MTBFs

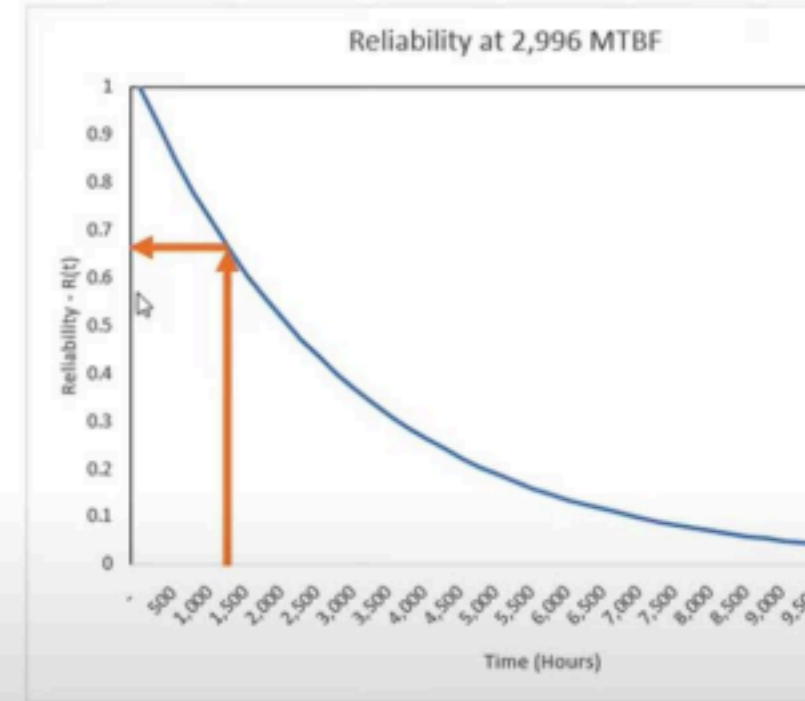
We've tested 20x units and found that our MTBF is 2,996 Hours. What is the reliability of our product at **1,200 hours of operation?**

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$$R(t) = e^{-\lambda t} = e^{-\frac{1}{\theta}(t)}$$

$$\text{Failure Rate} = \lambda = \frac{1}{\theta}$$

$$R(1,200) = e^{\frac{-1,200}{2,996}} = .6699$$



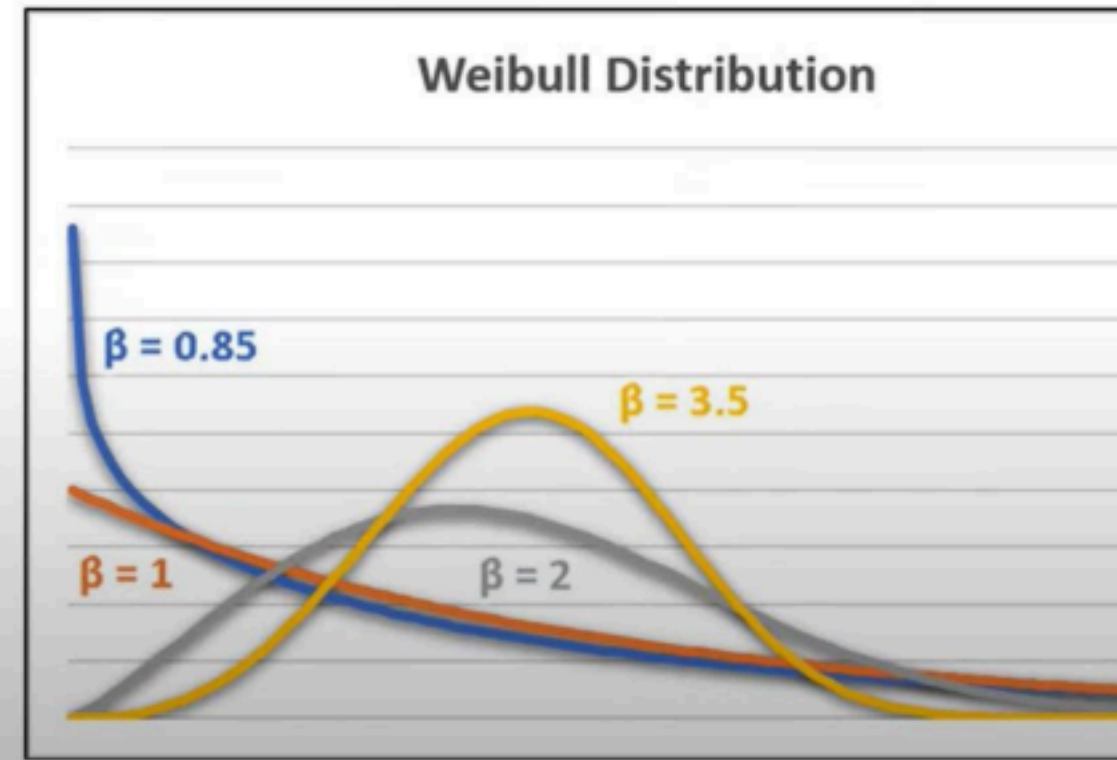
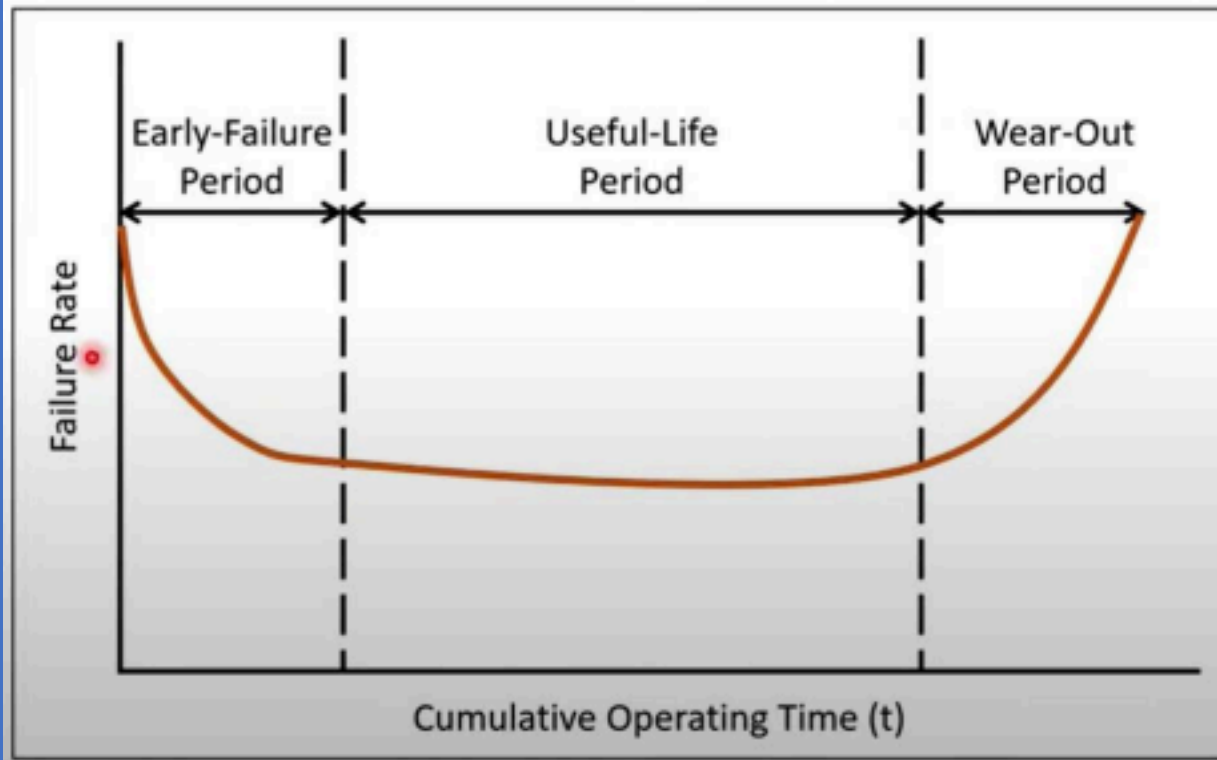
The probability that our product will perform successfully past the 1,200 hour mark is approximately 66%

**Alternative interpretation:** 66% of the population of units can be expected to surpass the 1,200 hour mark



# The Weibull Distribution

The weibull distribution was discovered by **Waloddi Weibull** and is the most **versatile** distribution in Reliability Engineering because of its ability to **model a variety of distributions**.

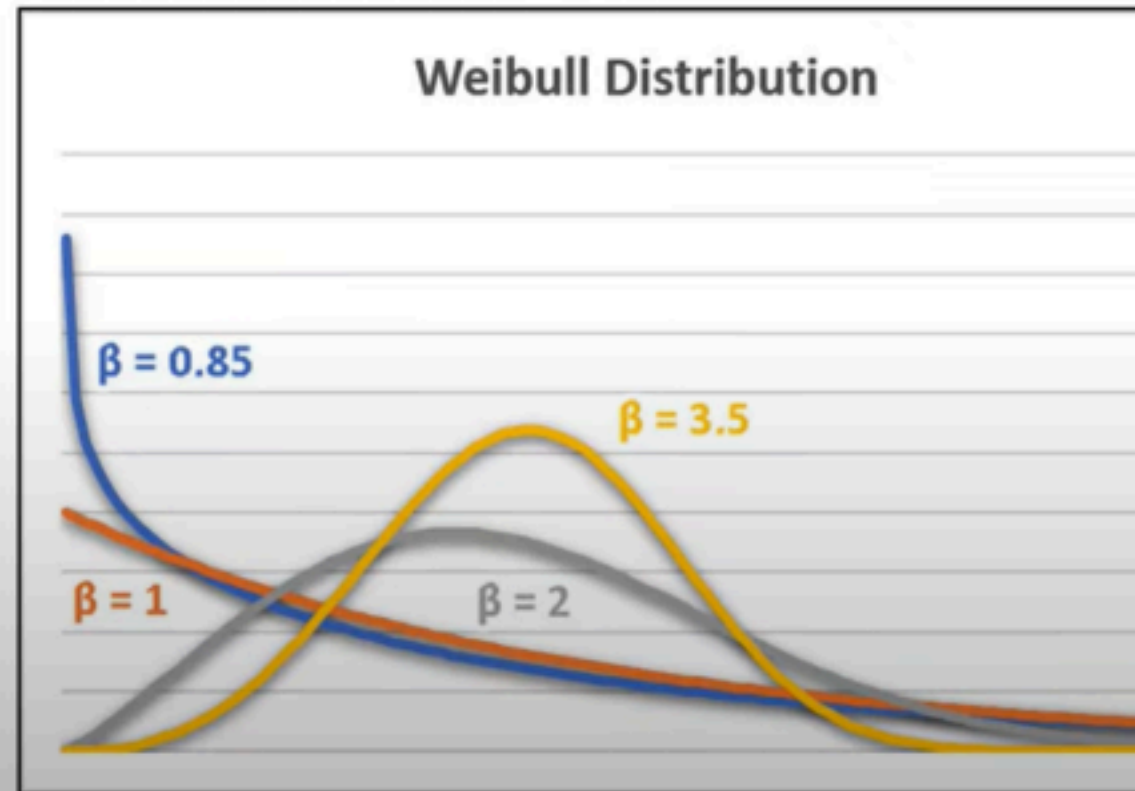


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*Reliability:*  $R(t) = e^{-\left(\frac{t}{\theta}\right)^{\beta}}$

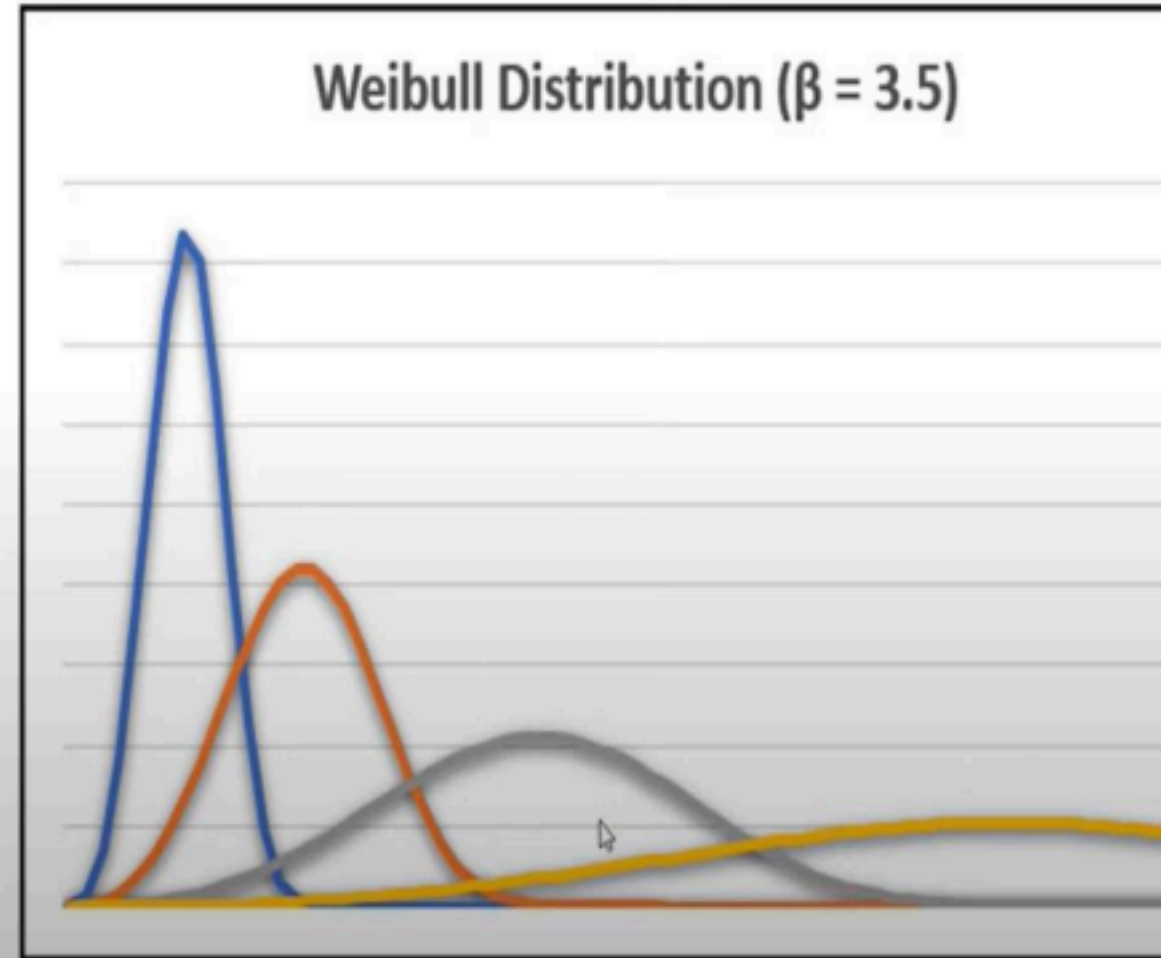
$\beta$  (**Beta**) - the Weibull **Shape** Parameter



Reliability:  $R(t) = e^{-\left(\frac{t}{\theta}\right)^{\beta}}$

$\beta$ (Beta) - the Weibull **Shape** Parameter

$\theta$ (Theta) - the Weibull **Scale** Parameter



# The Shape (Slope) Parameter

When  $\beta < 1$ , the weibull distribution represents a system with a **decreasing failure rate**

When  $\beta = 1$ , the weibull distribution is approximately equal to the **exponential distribution**

When  $\beta > 1$ , the weibull distribution represents a system with an **increasing failure rate**









[https://www.youtube.com/playlist?list=PLeo7Pn9luLrW6-lexh\\_ilb2K2uUeb3ssX](https://www.youtube.com/playlist?list=PLeo7Pn9luLrW6-lexh_ilb2K2uUeb3ssX)